• We proved the following in previous lectures -

 $L_d$  is not a TRL,  $\overline{L_d}$  is an undecidable TRL

 $L_u$  is an undecidable TRL.

since  $L_u$  is an undecidable TRL,  $\overline{L_u}$  is not a TRL

•  $L_u \leq_m L_{halt}$ 

 $f(\langle M, w \rangle) = \langle M', w \rangle$ , where M' is same as M except that M' loops when M reaches reject state hence,  $L_{halt}$  is undecidable

however, we proved that  $L_{halt}$  is a TRL via constructing a UTM

since  $L_{halt}$  is an undecidable TRL,  $\overline{L_{halt}}$  is not a TRL

•  $L_u \leq_m L_{equal}$ 

 $f(\langle M, w \rangle) = \langle M_1, M_2 \rangle$ , where

 $M_1$ : on input w' accept w'

 $M_2$ : on input w'', if M accepts w, accept w''

hence,  $L_{equal}$  is undecidable

•  $L_u \leq_m L_{regular}$ 

f(< M, w >) = < M' >, where

M': on input w'

if  $w' \in \{0^i 1^i | i \ge 0\}$  accept w'

else if M accepts w accept w'

hence,  $L_{regular}$  is undecidable

•  $\overline{L_u} \leq_m L_{finite}$ 

f(< M, w>) = < M'>, where

M': on input w'

if M accepts w accept w'

f(< M, w >) = < M' >, where

hence,  $L_{finite}$  is not a TRL

•  $\overline{L_u} \leq_m L_{empty}$ 

M': on input w'

- if M accepts w accept w'
- hence,  $L_{empty}$  is not a TRL
- $L_{empty} \leq_m L_{equal}$ 
  - $f(< M >) = < M, M^\prime >,$  where
  - M': on input w'

reject w'

hence,  $L_{equal}$  is not a TRL

since L<sub>u</sub> ≤<sub>m</sub> L<sub>equal</sub> (see above), L<sub>u</sub> ≤<sub>m</sub> L<sub>equal</sub>
hence, L<sub>equal</sub> is not a TRL