- 1. An IITian is *smart* if there exists some day N of his (indefinite) stay in IIT such that for any day $n \ge N$, the IITian solves tutorial sheet problems on day n. Who is a non-smart IITian?
- 2. An IITian is super smart if there exists some day N of her stay in IIT such that for any day $n \ge N$, if n is a working day, the IITian solves tutorial sheet problems on day n. Who is a non-super smart IITian?
- 3. Examples of graphs of functions with and without breaks at a certain point of their domain.
- 4. (SC) Sequential criterion: for every sequence $x_n \to c$, assuming $x_n \in \text{domain}(f)$, it should be true that $f(x_n) \to f(c)$. OPP.(SC): there exists a sequence $x_n \to c$ such that $x_n \in \text{domain}(f)$ but $f(x_n) \not\to f(c)$.
- 5. (WC) Weierstrass criterion: for any real $\epsilon > 0$, there exists a real $\delta > 0$ such that for every x satisfying $|x c| < \delta$, if $x \in \text{domain}(f)$, it should be true that $|f(x) f(c)| < \epsilon$. OPP. (WC): there exists a real $\epsilon_0 > 0$ such that for any real $\delta > 0$, there exists an $x_{\delta} \in \text{domain}(f)$ which satisfies $|x_{\delta} - c| < \delta$ but it is true that $|f(x_{\delta}) - f(c)| \ge \epsilon_0$.
- 6. Proof of OPP.(WC) implies OPP.(SC). This proves (SC) implies (WC).
- 7. Proof of (WC) implies (SC).
- 8. Domain: A subset $A \subset \mathbb{R}$ is a *domain* if for every $c \in A$, at least one one of the following three types of sets $[c, c + \alpha_0), (c \alpha_0, c + \alpha_0)$ or $(c \alpha_0, c] \subset A$ for some real $\alpha_0 > 0$.
- 9. Suppose $f : A \to \mathbb{R}$ is a function on a domain A. Say f is continuous at c by (SC) \equiv (WC). Say f is continuous if it is continuous at every point of its domain.
- 10. In domain(f), 'domain' associates an object to a function f. In a subset $A \subset \mathbb{R}$ being a domain, 'domain' is an adjective for subsets of reals.
- 11. Proof that the constant, identity and square functions are continuous by (WC).
- 12. Exercise: continuity of power, modulus, exponential and root functions.

- 1. Rules about continuity of resultant function at a point/over domain with respect to operations of addition, subtraction, multiplication, division and composition.
- 2. Applications: Continuity of polynomial and rational functions.
- 3. Non-traditional functions like Dirichlet's and Thomae's examples.
- 4. Thousand Dollar Challenge: Find a function from reals to reals which is discontinuous at irrationals and continuous at rationals.
- 5. A function is *bounded* if its range is bounded. *Supremum of a function* is the supremum of its range. Likewise infimum.
- 6. A function has an absolute maximum if it attains its supremum. Likewise for absolute minimum.
- 7. Examples for functions which are unbounded and do not attain their sup/inf on \mathbb{R} , on half-rays, on bounded intervals of various kinds.
- 8. Failure to produce such examples on intervals of type [a, b] for real $a \leq b$.